

Quark-lepton complementarity,
neutrino and standard model data

predict $\theta_{13}^{\text{PMNS}} = 9_{-2}^{+1} \text{ deg}$

Paris, Planck '06

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Quark-Lepton complementarity

- Neutrino experiments confirm that the **PMNS** lepton mixing matrix contains large mixing angles:
 - atmospheric mixing $\theta_{23}^{\text{PMNS}}$ is compatible with **45 deg**;
 - the solar mixing $\theta_{12}^{\text{PMNS}}$ is approx **34 deg**.
- To be compared with $\theta_{13}^{\text{PMNS}}$ and the mixing angles in the **CKM** matrix.
- The disparity between quark and lepton mixing angles has been viewed in terms of a 'quark-lepton complementarity' (**QLC**) which can be expressed in the relations

$$\theta_{12}^{\text{PMNS}} + \theta_{12}^{\text{CKM}} \simeq 45 \text{ deg}$$

$$\theta_{23}^{\text{PMNS}} + \theta_{23}^{\text{CKM}} \simeq 45 \text{ deg}$$

Correlation matrix

Definition

- Possible consequences of **QLC** have been investigated in the literature and in particular a simple correspondence between the **PMNS** and **CKM** matrices has been proposed and analyzed in terms of a correlation matrix.
- The correlation matrix is simply defined as the product of the **CKM** with the **PMNS** matrices
- There are unknown phases

Correlation matrix

Zero order approximation

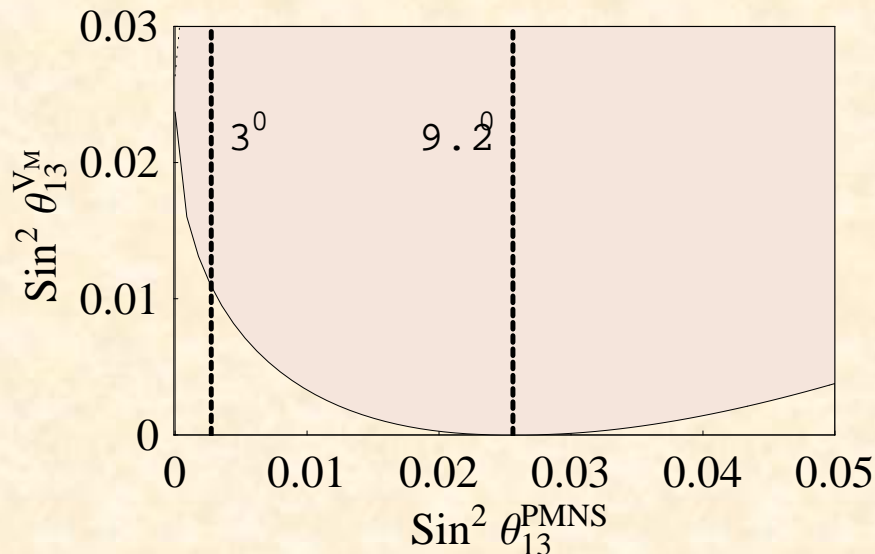
- For central values of the experimental data the (1,3) entry of the correlation matrix is not zero.
- To include particular correlation matrix
 - bimaximal (two angles of 45 deg and a vanishing one)
 - tribimaximal (one angle of 45 deg, one with $\tan^2 \theta = 0.5$ and a third vanishing one)

one needs models with renormalization effects
(relevant only for large $\tan \beta$ and quasi degenerate ν)

Correlation matrix

First order approximation

- Owing to the uncertainty in the value for $\theta_{13}^{\text{PMNS}}$, the (1,3) entry of correlation matrix may or may not include zero.

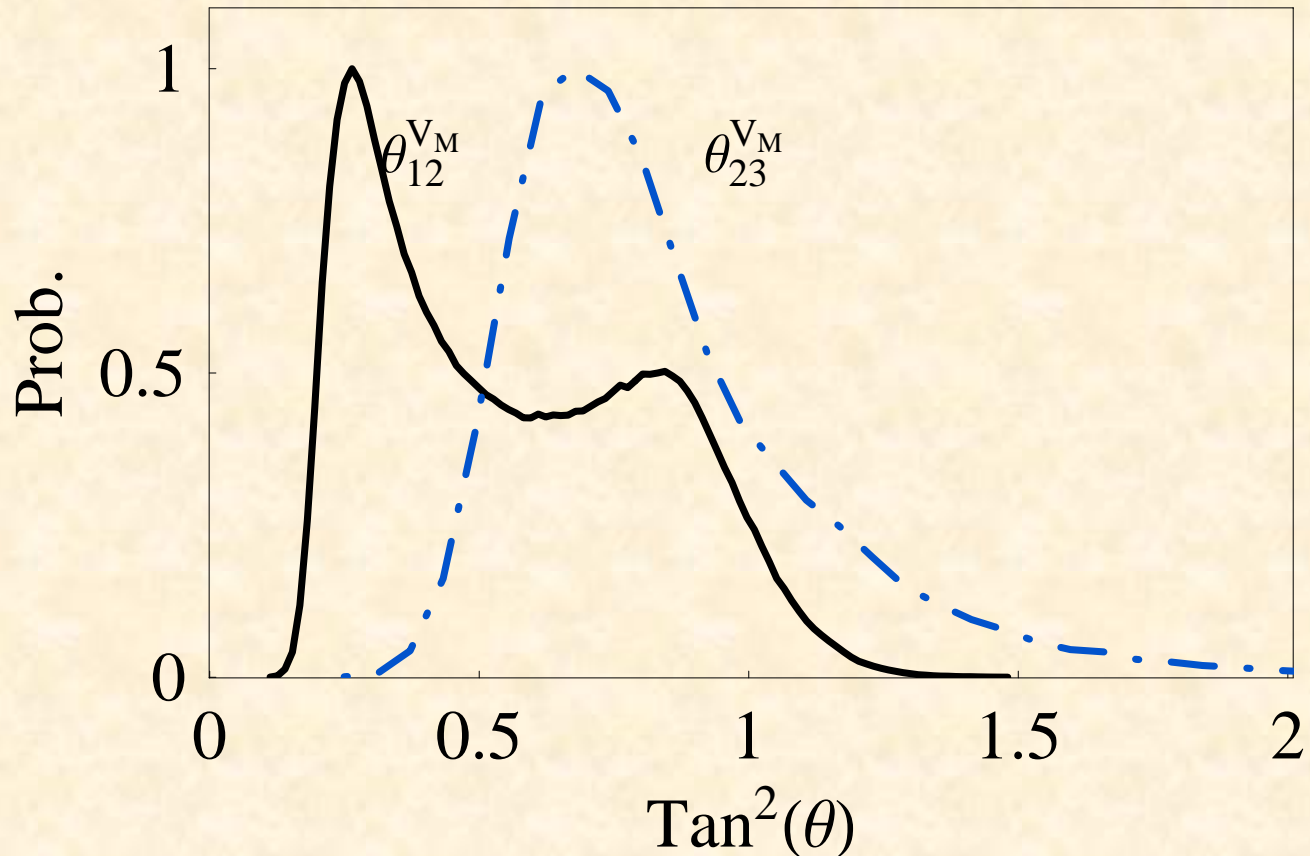


All the other **CKM** and **PMNS** mixing parameters are fixed at their best fit points.

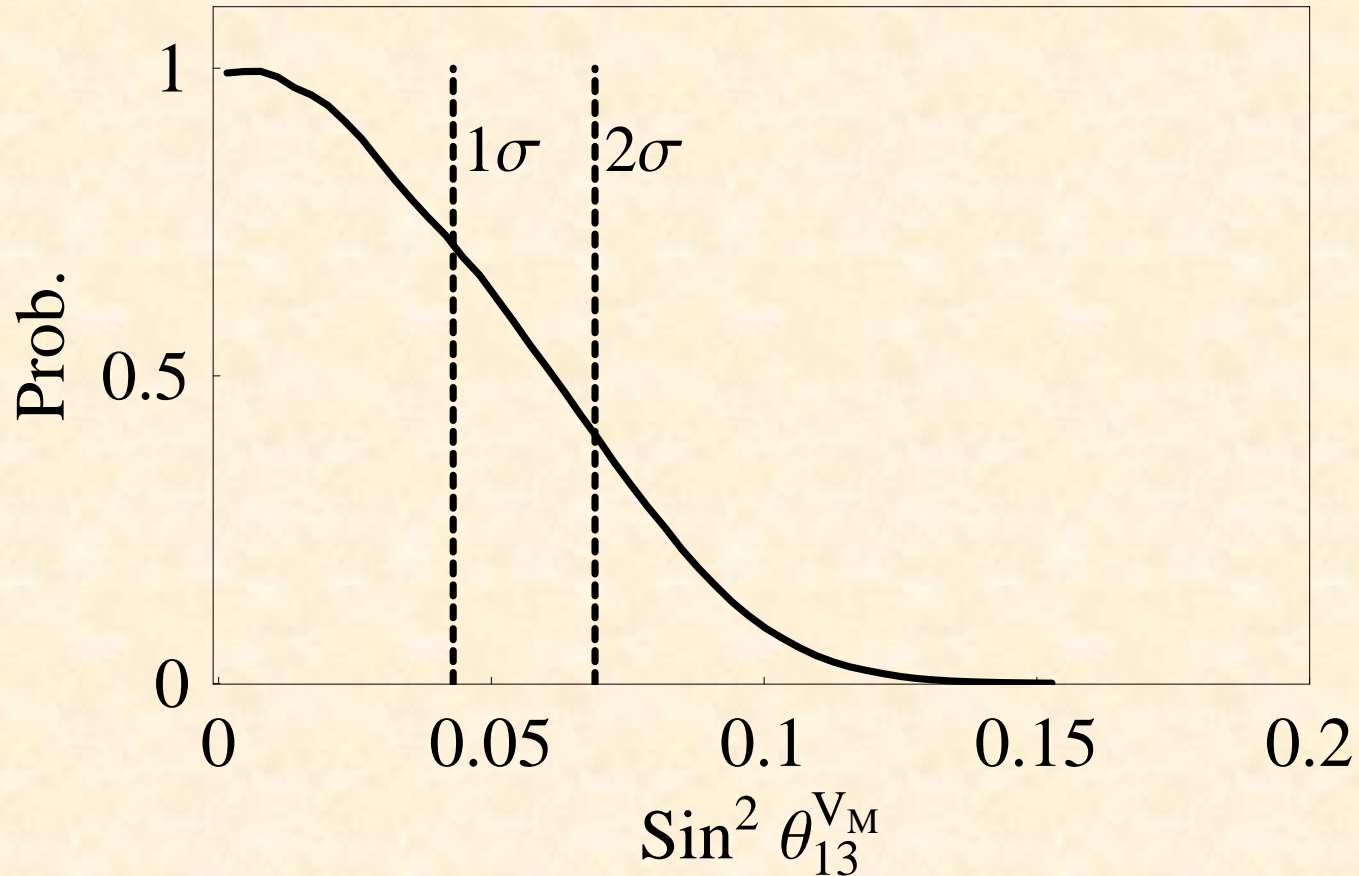
Bottom up approach

- We use all the **experimental data** with their uncertainty in a Monte Carlo simulation to convolute them
- The correlation matrix **CKM * PMNS** has:
 - $0.3 < \tan^2 \theta_{12} < 1.$
 - $0.5 < \tan^2 \theta_{23} < 1.4$
 - $\sin^2 \theta_{13} < 0.1$

Correlation matrix: θ_{12} and θ_{23}



Correlation matrix: θ_{13}

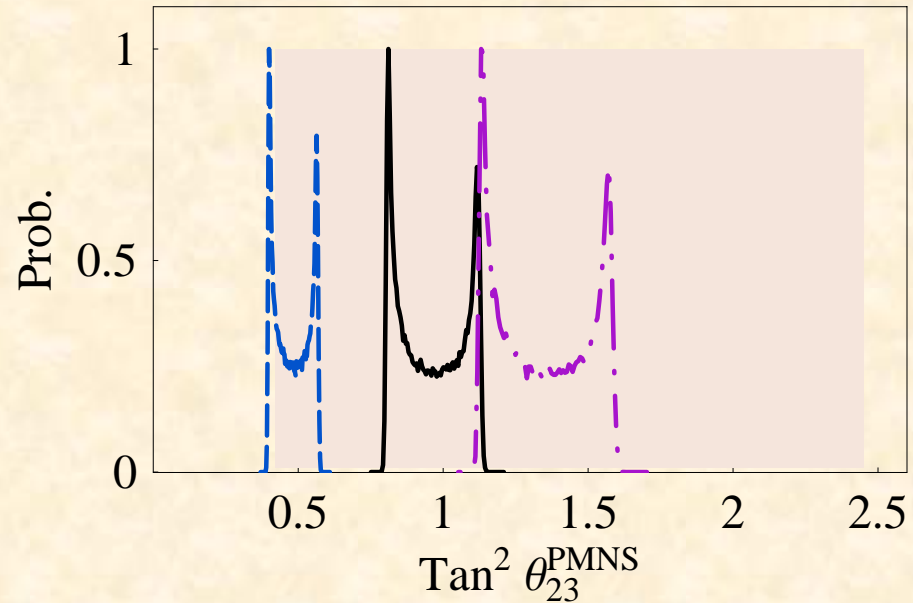
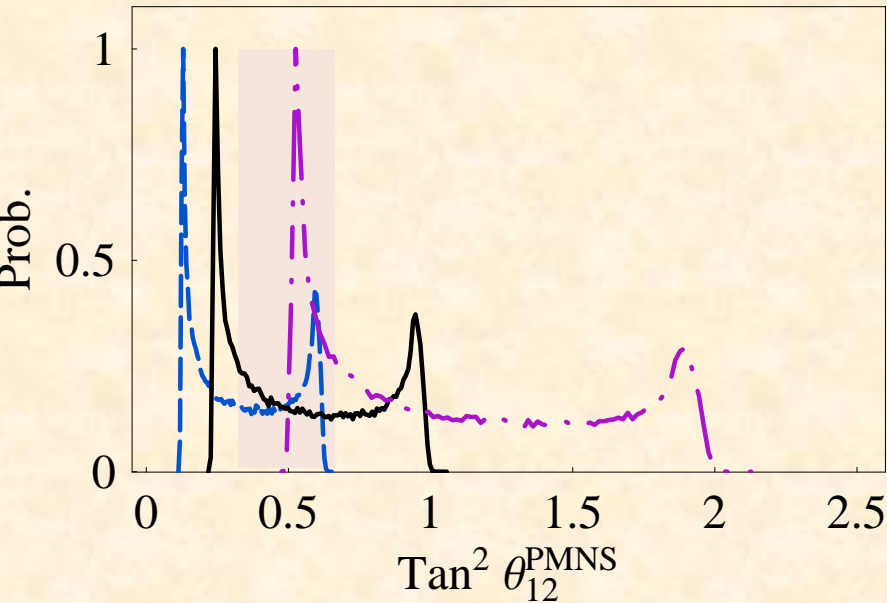


Top down approach

- If we assume that the correlation matrix has:
 - $0.3 < \tan^2 \theta_{12} < 1.$
 - $0.5 < \tan^2 \theta_{23} < 1.4$
 - $\sin^2 \theta_{13} = 0 < \text{----- Hypotesis}$

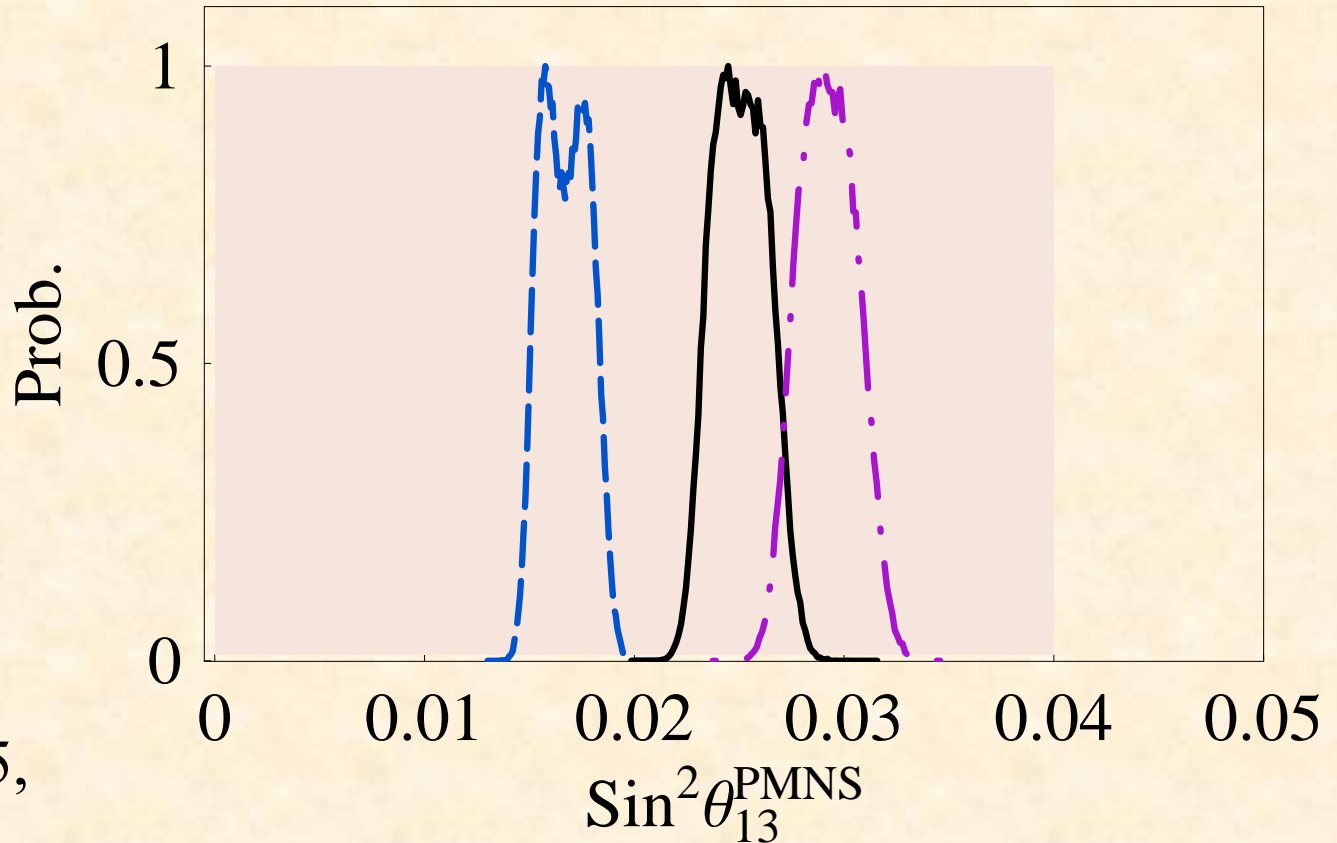
then we get that the unknow mixing lepton angle $\theta_{13}^{\text{PMNS}}$ is 9_{-2}^{+1} deg.

PMNS matrix: $\theta_{12}^{\text{PMNS}}$ and $\theta_{23}^{\text{PMNS}}$



- (left) $\tan^2 \theta_{23} = 1.0$, $\sin^2 \theta_{13} = 0$,
 $\tan^2 \theta_{12} = 0.3$ (dashed), 0.5 (continuous), 1.0 (dot-dashed)
- (right) $\tan^2 \theta_{12} = 0.5$, $\sin^2 \theta_{13} = 0$,
 $\tan^2 \theta_{23} = 0.5$ (dashed), 1.0 (continuous), 1.4 (dot-dashed)

PMNS matrix: $\theta_{13}^{\text{PMNS}}$

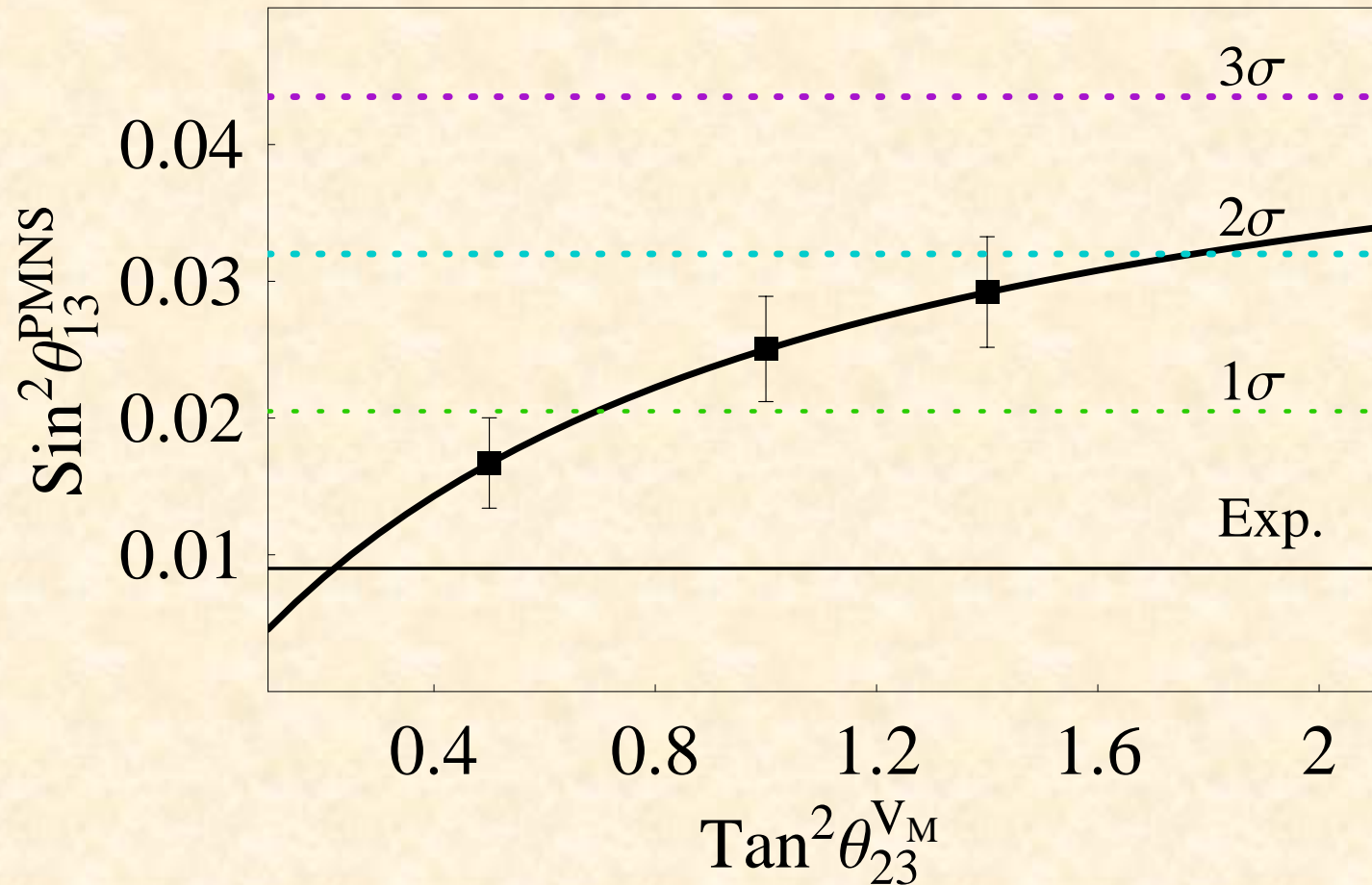


$$\tan^2 \theta_{12} = 0.5,$$

$$\sin^2 \theta_{13} = 0,$$

$$\tan^2 \theta_{23} = 0.5 \text{ (dashed), } 1.0 \text{ (continuous), } 1.4 \text{ (dot-dashed)}$$

$\sin^2 \theta_{13}^{\text{PMNS}}$ as a function of $\tan^2 \theta_{23}$



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